

# Simulation Modeling of Manufacturing System in Relation to Route Flexibility Degree, Open Rate of Operations and Production Type

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**Abstract**—In the paper the influence of route flexibility degree, open rate of operations and production type coefficient on makespan is discussed. The flexible job-open shop scheduling problem FJOSP (an extension of the classical job shop scheduling) is analyzed. For the analysis of the production process the GRASP (greedy randomized adaptive search procedure) and simulated annealing heuristic algorithms were used. Experiments with different levels of factors have been considered and compared. The presented algorithms have been tested, and illustrated with examples for serial route.

**Index Terms**—Makespan, open shop, route flexibility, simulation modeling, type of production.

## I. INTRODUCTION

Simulation modeling [1]-[17] is a common paradigm for analyzing complex systems. The greatest overall benefit of using simulation in a manufacturing environment is that it allows a manager or engineer to obtain a system wide view of the effect of “local” changes to the manufacturing system. There are a number of specific potential benefits from using for manufacturing analyses, including [11]:

- increased throughput (parts produced per unit of time)
- decreased times in system of parts
- reduced in-process inventories of parts
- increased utilization of machines or workers
- increased on-time deliveries of products to customers, etc.

Simulation is well known as a powerful tool supporting the design, layout or re-design of production systems. Recently, many successful applications proved that it can also support the operation of manufacturing systems, especially in the area of scheduling and control.

Almost in large, and the majority of small and medium-sized enterprises run MRP/ERP systems. However, many are not satisfied with their systems.

There are a number of other well-known [18]-[25], general-purpose simulation packages, including AnyLogic [26], GPSS/H [18], HyPerformix Workbench [22], MicroSaint [23], SIMSCRIPT III [19], SIMUL8 [20],[25], SLX [21].

Several simulation products such as Simulik, ACSL, and Dymola have been specifically designed for building continuous simulation models. In addition, Discrete Event simulation packages Arena [15] and Extend [10] have continuous modeling capabilities.

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We list [27]-[33] some of the application-oriented simulation packages that are currently available which are used in manufacturing and supply chain: Simulation Dynamics [33], AutoMod [27], Enterprise Dynamics, Flexsim [29], PROMODEL [30],[32], QUEST [28], Witness [31].

The broad goal of manufacturing operation management, such as a resource constrained scheduling problem, is to achieve a coordinated efficient behaviour of manufacturing in servicing production demands, while responding to changes on shop-floors rapidly and in a cost effective manner. Shop floor scheduling, such as resource constrained scheduling problems in general, is a combinatorially complex, NP-hard problem, thus is unfeasible to be solved computationally by the sole use of conventional operations research approaches.

The development of decision-making methodologies is currently headed in the direction of simulation and search algorithm integration. This leads to a new approach, which successfully joins simulation and optimization. Artificial Intelligence based or hybrid techniques using domain specific heuristics are necessary to guide the search and to provide satisfactory solutions in due time [34]-[42].

The paper is organized as follows. Section 2 formulates the problem. In section 3 the dependency of makespan on the flexibility of route, open rate of operations and production type coefficient for serial route have been described. The concluding remarks are given in section 4.

## II. PROBLEM FORMULATION

The  $n \times m$  classical job shop scheduling problem (JSP) involves  $n$  jobs and  $m$  machines. Each job is to be processed on each machine in a predefined sequence. We consider of the flexible open - shop scheduling problem.

In an open shop scheduling problem (OSP), a set of  $n$  jobs  $I_1, I_2, \dots, I_n$  has to be processed on a set of  $m$  machines  $M_1, M_2, \dots, M_m$ . The processing of a job on machine is denoted as an operation, and the sequence in which the operations of a job are processed on the machines is immaterial.

Flexible job shop scheduling problem (FJSP) extends the JSP by allowing each operations to be processed on more than machine. With this extension, we are now confronted with two subtask: assignment of each operation to an appropriate machine and sequencing operations on each machine.

The FJOSP is formulated as follows. There is a set of jobs  $Z = \{Z_i\}$ ,  $i \in I$ , where  $I = \{1, 2, \dots, n\}$  is an admissible set of parts,  $U = \{u_k\}$ ,  $k \in 1, m$ , is a set of machines. Each job  $Z_i$  is a group of parts  $I_i$  of equal partial task  $p_i$  of a certain range of

production. Operations of technological processing of the  $i$ -th part are denoted by  $\{O_{ij}\}_{j=\xi}^{H_i}$ . Then for  $Z_i$ , we can write  $Z_i = (\Pi_i \{O_{ij}\}_{j=\xi}^{H_i})$ , where  $O_{ij} = (G_{ij}, t_{ij(N)})$  is the  $j$ -th operation of processing the  $i$ -th group of parts;  $\xi_i$  is the number of operation of the production process at which one should start the processing the  $i$ -th group of parts;  $H_i$  is the number of the last operation for a given group;  $G_{ij}$  is a group of interchangeable machines that is assigned to the operation  $O_{ij}$ ;  $G$  is a set of all groups of machines arose in the matrix  $\|\{Z_i\}\|$ ;  $t_{ij(N)}$  is an elementary duration of the operation  $O_{ij}$  with one part  $d_i$  that depends on the number of machine  $N$  in the group (on the specified operations);  $t'_{ij}$  is the duration of set up before the operation  $O_{ij}$ ;  $N_{gr}$  is the number of all groups of machines. In this problem the sequence in which the operations of a job are processed on the machines is immaterial (with different open rates of operations). The most widely used objective is to find feasible schedules that minimize the completion time of the total production program, normally referred to as makespan ( $C_{max}$ ). In this paper the dependency of makespan on the route flexibility degree, open rate of operations and production type coefficient for serial route have been described. The algorithm SA+GRASP [43-44] for the optimization of the production process has been used.

### III. COMPUTER EXPERIMENTS

If a model has only one factor, the experimental design is simple: we just run the simulation at various values, or levels, of the factor, perhaps forming a confidence interval for the expected response at each of the factor levels.

In this experiment there are  $k = 3$  factors and we want to get an initial estimate of how each factor affects the response. We might also want to determine if the factors interact with one another, i.e., whether the effect of one factor on the response depends on the levels of the others. On way to measure the effect of a particular factor would be to fix the levels of the other  $k-1$  factors at some set of values and make simulation runs at each of two levels of the factor of interest to see how the response reacts to changes in this single factor. A much more economical strategy for determining the effects of factors on the response with which we can also measure interactions, called a  $2^k$  factorial design, requires that we choose just two levels for each factors and then calls for simulation runs at each of the  $2^k$  possible factor-level combinations, which are sometimes called design points. Because we are using only two levels for each factor, we assume that that the response is approximately linear over the range of the factor.

In this work we examined open job problem defined in such a way that an operation (of the same type) of a job can be performed on any machine of changeable machines group (CMG) and the sequence in which the operations are processed on the machines is immaterial. The open rate of process  $O$  was defined as the number of operations in a process can be performed with immaterial sequence. For example, let there be 10 operations for given part. If two operations can be performed on any machine in the CMG group and sequence in which these operations are processed

is immaterial then the open rate is  $2/10 = 0.2 = 20\%$ . In this paper the following open rates were used  $O$ : 6%, 13%, 19%, 25%, 31%, 38%, 44%, 50%, 56%, 63%, 69%, 75%, 81% and 100%.

The route flexibility defined in such a way that an operation of the same type can be performed on any machine of changeable machines group. The flexibility rate  $E$  was defined as the number of machines in a group capable of performing a given operation. For example, let there be 10 changeable machines divided into 5 groups of two machines. If a given operation can be performed on any machine in the CMG group, then the flexibility rate is  $2/10=0.2$ . In this work the following route flexibility rates were used  $E$ : 0.2; 0.4; 0.6; 0.8 and 1.0.

We can use value of production type coefficient  $K_{tp}$ , which is described:

$$K_{tp} = \frac{\sum_{i=1}^m P_o \times F \times K_o}{\sum_{i=1}^n N_i \times t_i} \quad (1)$$

where:  $\sum_{i=1}^m P_o$  - general number of production operations that were used at  $i$  working position in a month,  $i \in 1, m$ ;  $F$  - a fund of work time in a month;  $N_o$  - an average coefficient of a norm execution;  $N_i$  monthly program of  $i$  assortment;  $t_i$  - labor of  $i$  assortment;  $n$  - a number of products assortment. With coefficient  $K_{tp}$  (further marked with the symbol  $k$ ) we can show relationships between a type of process, a form of process organization, and a kind of production system technical base [45]. In a serial route an entire batch of parts is processed on one machine and only when all of the products in the batch have been processed are they sent to the next machine.

#### A. Experiments with 3 Factors (Variant 1)

For the experiment with one factor, the  $C_{max}$  value increased, when the open rate changed as follows: O1'-100%, O2'-44% and  $C_{max}$  value increased, when the flexibility degree changed in the following sequence: E1'-0,2; E2'-1, E3'-0,4. The experiments with the  $k$  coefficient proved that the  $C_{max}$  increased when the  $k$  value decreased as follows: k1'-32, k2'-19, k3'-7 (as shown in Table 1).

TABLE I:  $C_{MAX}$  VALUES FOR THE EXPERIMENT WITH ONE FACTOR

Experiment	Open rate, flexibility degree, coefficient k	level sign	makespan average [min]
Open rate	0-15 (100%)	O1'	15178,42
	0-6 (44%)	O2'	40381,55
	0 (0%)	O3'	53649,13
Flexibility degree	0,2	E1'	50242,2
	1,0	E2'	50397,28
	0,4	E3'	51926,76
Coefficient k	32	k1'	24536,44
	19	k2'	27682,94
	7	k3'	50666,84

The three-factor experiments carried-out show the influence of the factors (flexibility degree  $E$ , open rate  $O$ , coefficient  $k$ ) on the makespan  $C_{max}$  value (Table 2).

The experiments proved that the  $C_{max}$  values do not always increase when the open rate increases, as was the case with the one-factor experiment (in the sequence O1', O2', O3'). For the open rate O1, the  $C_{max}$  values are the lowest

(regardless of the flexibility degree  $E$  and the  $k$  coefficient). However for the other two levels of the open rate, the  $C_{max}$  values depend on the  $E$  flexibility degree and/or the  $k$  coefficient.

TABLE II:  $C_{MAX}$  VALUES FOR EXPERIMENT WITH THREE FACTORS (FLEXIBILITY DEGREE, OPEN RATE,  $k$  COEFFICIENT)

Experiment	open rate level	Open rate value	Flexibility degree level	Flexibility degree value	Coefficient k level	Coefficient k value	Makespan value			
							average	change	min	max
1	O1	0-15	E1	0,2	O1k1	32	18940,8	-	18940,8	18940,8
2	O1	0-15	E1	0,2	O1k2	19	18940,8	0,00%	18940,8	18940,8
3	O1	0-15	E1	0,2	O1k3	7	19213,1	1,44%	18940,8	19572,9
4	O1	0-15	E2	1	k1	32	14063,6	-26,80%	14054,4	14071,5
5	O1	0-15	E2	1	k2	19	13458,6	-4,30%	13448,6	13472,3
6	O1	0-15	E2	1	k3	7	13066,3	-2,91%	12921,8	13273,2
7	O1	0-15	E3	0,4	k1	32	14100,7	7,92%	14065,5	14129,9
8	O1	0-15	E3	0,4	k2	19	13741,7	-2,55%	13525,9	13831,1
9	O1	0-15	E3	0,4	k3	7	14890,1	8,36%	14038,7	15612,4
10	O2	0-6	E1	0,2	O2k1	32	26413,2	77,39%	26080,3	26709,3
11	O2	0-6	E1	0,2	O2k2	19	28185,3	6,71%	27591,3	28527,9
12	O2	0-6	E1	0,2	O2k3	7	44505,2	57,90%	44378,3	44781,4
13	O2	0-6	E2	1	k1	32	21170,8	-52,43%	20957,3	21381,3
14	O2	0-6	E2	1	k2	19	24446,1	15,47%	24059,4	24721,9
15	O2	0-6	E2	1	k3	7	42790,3	75,04%	41620,9	43482,1
16	O2	0-6	E3	0,4	k1	32	23034,4	-46,17%	22866,2	23228,0
17	O2	0-6	E3	0,4	k2	19	25820,0	12,09%	25442,1	26056,2
18	O2	0-6	E3	0,4	k3	7	44100,2	70,80%	42924,0	44763,5
19	O3	0	E1	0,2	O3k1	32	28084,1	-36,32%	27738,8	28642,6
20	O3	0	E1	0,2	O3k2	19	32021,4	14,02%	31461,5	32466,2
21	O3	0	E1	0,2	O3k3	7	53358,2	66,63%	53358,2	53358,2
22	O3	0	E2	1	k1	32	22611,5	-57,62%	22511,3	22671,0
23	O3	0	E2	1	k2	19	27276,7	20,63%	26711,2	27910,9
24	O3	0	E2	1	k3	7	53923,8	97,69%	53358,2	55428,6
25	O3	0	E3	0,4	k1	32	24709,1	-54,18%	24050,8	25058,6
26	O3	0	E3	0,4	k2	19	28715,2	16,21%	28284,2	29105,1
27	O3	0	E3	0,4	k3	7	57350,3	99,72%	54612,8	59514,9

The  $C_{max}$  value is always lower for level O2 than O3, but only when we take into account the same levels of the flexibility degree and of the  $k$  coefficient. Therefore it can occur that with the same  $k$  coefficient and different flexibility degrees, the  $C_{max}$  values will be lower for level O3 than O2 (for example: with the same k1 level the  $C_{max}$  value for O3 and E3 is lower than the  $C_{max}$  value for O2 and E1). Similarly with the same flexibility degree, the  $C_{max}$  value for the O3 open rate can be lower than for level O2, while the  $k$  coefficient changes.

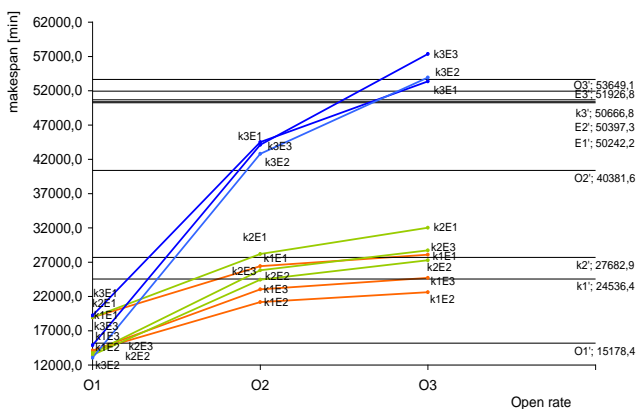


Fig. 1. Relationship between the  $C_{max}$  value and the open rate for various values of the flexibility degree and the  $k$  coefficient

For the experiment with one factor, the  $C_{max}$  values increased, when the  $k$  coefficient decreased (according with the sequence k1', k2', k3'). In case of the experiment with three factors (flexibility degree, open rate, the  $k$  coefficient) the  $C_{max}$  values did not increased when the  $k$  coefficient changed from k1 to k2 to k3. The maximum  $C_{max}$  value was

obtained at the k3 coefficient level on levels O2 and O3 of the open rate. On the other hand with the same k3 coefficient – the  $C_{max}$  values are the lowest when the open rate is O1.

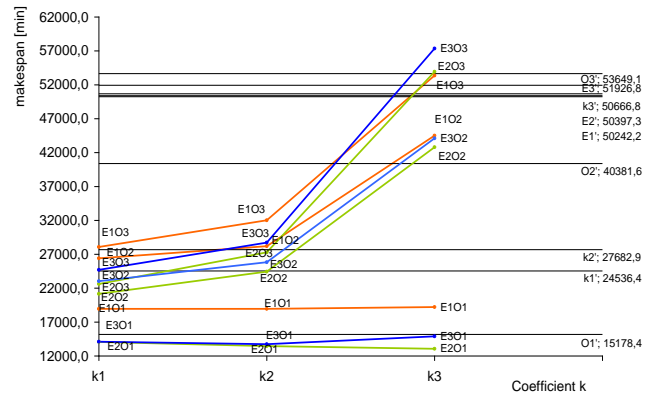


Fig. 2. Relationship  $C_{max}$  value and coefficient  $k$  for various values of open rate and flexibility degrees

For the experiment with one factor the  $C_{max}$  values increased when the flexibility degree is as follows: E1', E2', E3'. In the case of the three-factor experiment (flexibility degree, open rate, coefficient  $k$ ) the  $C_{max}$  values are various for various flexibility degree levels. The average minimum  $C_{max}$  value was obtained at the E2 flexibility degree level, and the maximum  $C_{max}$  values were obtained at the E3 flexibility degree level.

Considering the minimum and maximum  $C_{max}$  values for a given flexibility degree and open rate level it can be noticed that for levels O1, O2 and O3 levels the minimum  $C_{max}$  value was obtained at the E2 flexibility degree (i.e. differently than for the experiment with one factor, where the minimum  $C_{max}$  value was obtained at the E1' level). Moreover for the O1 and O2 open rates levels the maximum  $C_{max}$  was obtained at E1 (also differently than in the experiment with one factor, where the maximum  $C_{max}$  value was obtained at the E3'), while for O3 at the E3 level.

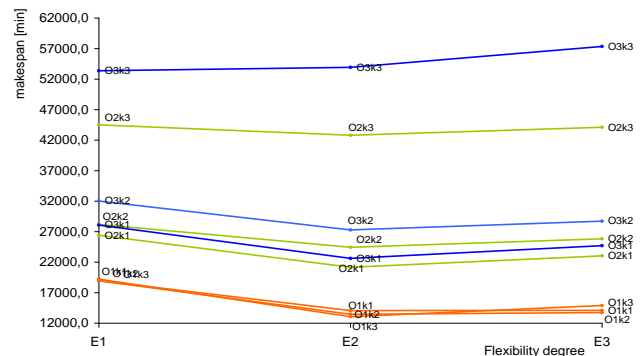


Fig. 3. Relationship  $C_{max}$  value and coefficient  $k$  for various coefficient  $k$  and open rate

The maximum  $C_{max}$  value was obtained at a combination of O3, E3, k3, and the minimum  $C_{max}$  value at the O1, E2, k3 combination. The worst result was obtained at the same combination of the factor levels as in the experiment with one factor. On the other hand the minimum  $C_{max}$  value for the experiment with three factors (flexibility degree, open rate, coefficient  $k$ ) was obtained only for one level in the

experiment with one factor i.e. at the O1 level. The other combinations proved that the  $C_{max}$  value should be worse, however the best result was obtained at the O1 level.

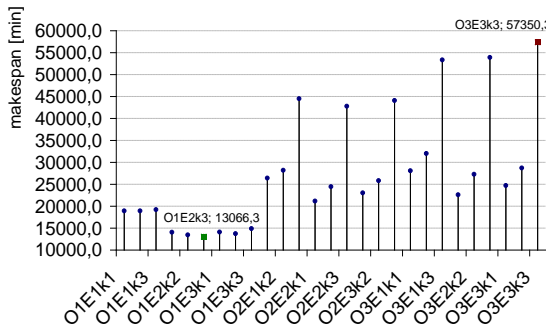


Fig. 4. Min and max  $C_{max}$  value in experiment with three factor (flexibility degree, open rate, coefficient  $k$ )

**B. Experiments with 3 Factors (Variant 2)**

Considering the fixed open rate the following relationships can be noticed (Fig. 5) For the O1 open rate level, the maximum  $C_{max}$  value was obtained for the E1 flexibility degree level, while the minimum  $C_{max}$  value - at the E2 flexibility degree level (although not in every case).

The value of the  $k$  coefficient does not influence the  $C_{max}$  value in a decisive way, because  $C_{max}$  values - small, medium, and large - were obtained for all levels of the  $k$  coefficient. For O2 and O3 open rate levels the  $k$  coefficient has great influence on the  $C_{max}$  value.

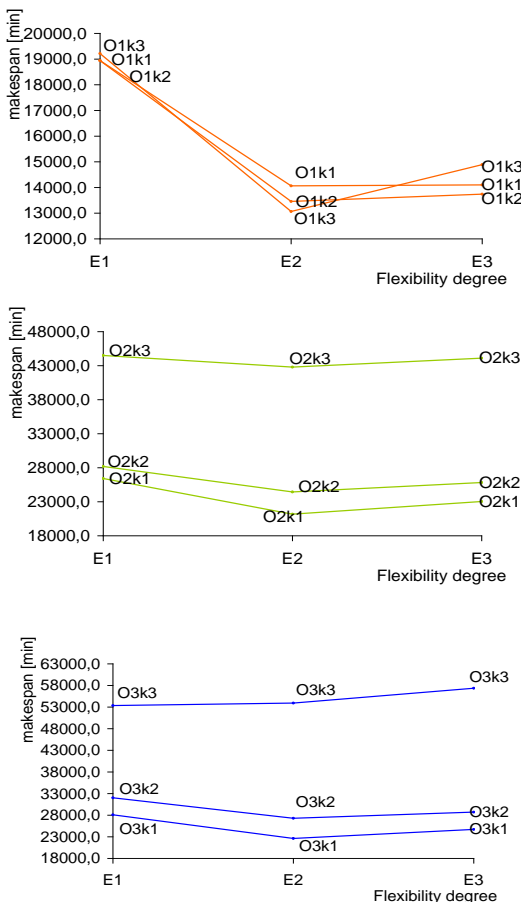


Fig. 5. Relationship between  $C_{max}$ , flexibility degree,  $k$  coefficient and the fixed O1, O2 and O3 open rate levels

When the  $k$  coefficient decreases (from  $k_1$  to  $k_3$ ), the  $C_{max}$  increases (as in the experiment with one factor when only the  $k$  coefficient is considered). The exception for the O2 open rate level is only one  $C_{max}$  value - with the combination O2,  $k_1$ , E1, at which the  $C_{max}$  value is greater than the value for the  $k_2$  level, i.e. with the combinations O2,  $k_2$ , E2 and O2,  $k_2$ , E3. The exception for the O3 open rate level is also one  $C_{max}$  value, with the O3,  $k_1$ , E1 combination, at which the  $C_{max}$  has a greater value than for the  $k$  coefficient, i.e. with the O3,  $k_2$ , E2 combination. Most  $C_{max}$  values which are obtained at O1, O2 and O3 open rate levels are lower than the values which were obtained in one-factor experiment (O1', O2' and O3' open rate levels respectively).

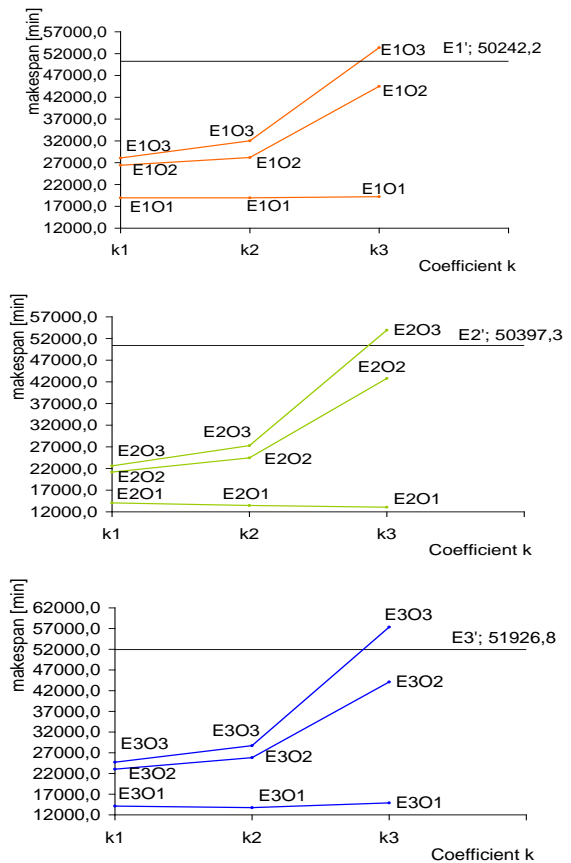


Fig. 6. Relationship  $C_{max}$ ,  $k$  coefficient, open rate and the fixed E1, E2 and E3 flexibility degree

Considering the flexibility degree as fixed the following dependencies can be noticed (fig. 6).

Considering the  $k$  coefficient as fixed the following dependencies can be noticed (fig. 7).

For all  $k$  coefficient levels, at O1 open rate level the minimum  $C_{max}$  value was always obtained. On the other hand for the  $k_3$  coefficient, at the O3 open rate level, the maximal  $C_{max}$  value is always obtained. The flexibility degree does not influence significantly the  $C_{max}$  value, because  $C_{max}$  values - small, medium, and large - were obtained for all levels of the  $k$  coefficient. However it can be noticed that at E2 the minimum  $C_{max}$  value is obtained, regardless of the  $k$  coefficient level. Most  $C_{max}$  values obtained at  $k_1$ ,  $k_2$  and  $k_3$  coefficient are lower than the values obtained in the experiment with one factor ( $k_1'$ ,  $k_2'$  and  $k_3'$  respectively).

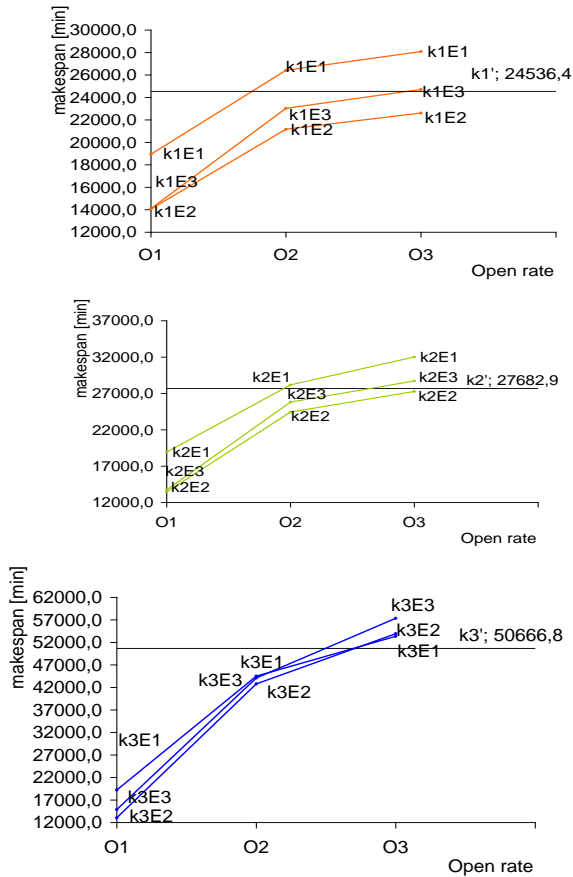


Fig. 7. Relationship  $C_{max}$ , open rate, the flexibility degree and the fixed  $k_1$ ,  $k_2$  and  $k_3$  coefficient.

#### IV. CONCLUSION

We proposed the use of SA+GRASP metaheuristic in the analysis of the production systems (for flexible job-open scheduling problem). The influence of route flexibility degree, open rate of operations and production type coefficient on makespan is discussed. Experiments with one and three factors have been tested and different levels of factors have been considered and compared. The algorithms have been implemented, tested, and illustrated with examples for the serial route.

As a future perspective, it will be interesting to compare the proposed approach with the other methods and carry out experiments for the parallel route and also to study the problem on a large set of benchmark data and real problems.

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